

**Behavioral Macroeconomics:
Part 4 - Hyperbolic Discounting and Savings**

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Macroeconomics and Saving

Golden Eggs and Hyperbolic Discounting (Laibson QJE 1997)

- Self-control problems → commitment (binding dead-lines, special bank accounts, health-clubs, diet)
- All illiquid assets provide a form of commitment (though there are other reasons to hold them such as diversification, higher expected returns), retirement plans, pension funds

Characterization of Hyperbolic Discounting Functions

- Relatively high discount rate over short horizons
- Relatively low discount rate over long horizons
- Example: from today's perspective, the discount rate between two far-off periods, t and $t + 1$ is the low long-term discount rate, but from time t perspective, the discount rate between t and $t + 1$ is the high short-term discount rate

Summary

Laibson's (1997) conclusions:

- Framework explains high correlation between consumption and income
- Consumers have different propensity to consume out of wealth than labor income
- Ricardian equivalence should not hold
- Financial innovation may have caused savings' decline in the U.S.
- Financial innovations reduce welfare by providing too much liquidity

The Model

- Time-additive utility function:

$$U_t = E_t[u(c_t) + \beta \sum_{\tau=1}^{T-t} \delta^\tau u(c_{t+\tau})] \quad (1)$$

- The discount structure is so called “quasi-hyperbolic” - the discount function is a discrete time function with values

$$\{1, \beta\delta, \beta\delta^2, \beta\delta^3, \dots\} \quad (2)$$

The Model (continued)

- Preferences given by equation (1) are dynamically inconsistent (preferences at date t are inconsistent with preferences at date $t + 1$)
- Marginal rate of substitution between time $t + 1$ and $t + 2$ at time t is $u'(c_{t+1})/\delta u'(c_{t+2})$
- Marginal rate of substitution at time $t + 1$ is $u'(c_{t+1})/\beta\delta u'(c_{t+2})$
- Analyzing equilibrium behavior when preferences are dynamically inconsistent: A T -period consumption problem \rightarrow a T -period game with T players or “selves” \rightarrow subgame perfect equilibrium

The Model (continued)

- Consumer has liquid assets x_{t-1} and nonliquid assets z_{t-1} , both chosen at time period $t - 1$. These yield gross return of $R_t = 1 + r_t$.
- Consumption is chosen from deterministic labor income and access to liquid savings $c_t \leq y_t + R_t x_{t-1}$. Note, that in the period of control, self t cannot consume the illiquid asset.
- Thereafter, consumer chooses new asset allocation $y_t + R_t(z_{t-1} + x_{t-1}) - c_t = z_t + x_t$ and $x_t, z_t \geq 0$.

The Model (continued)

- Consumer may borrow against his illiquid assets. Creditor gets contingent control right over some of those assets, consumer receives liquidity that can be consumed.

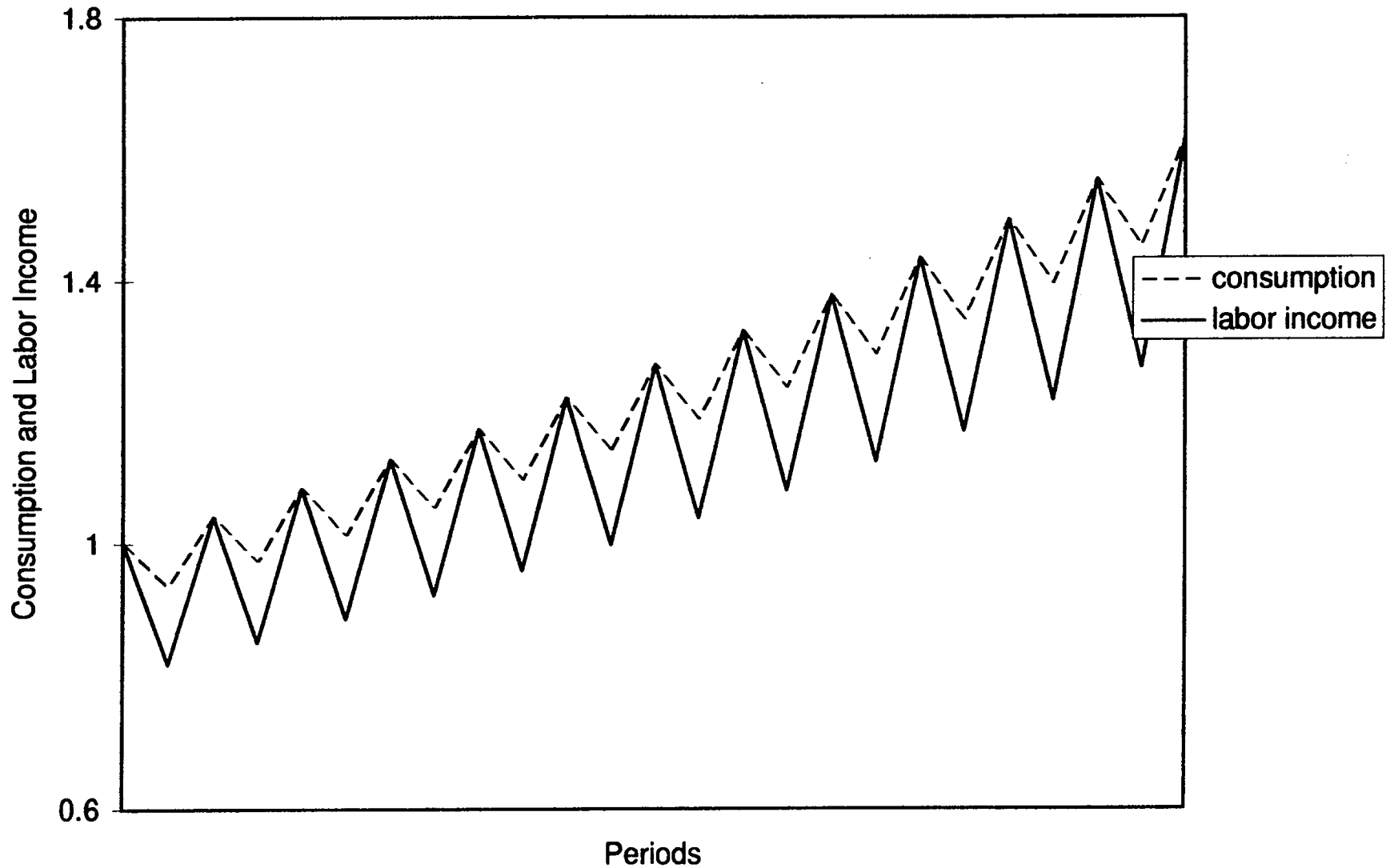
Co-Movement in Consumption and Income

- In the model, self $t - 1$ chooses x_{t-1} to constrain the consumption of self t . As such, manipulation of cash flow process by keeping most assets in the illiquid instrument
- Self-imposed liquidity constraint
- In equilibrium consumption equals current level of cash flow:

$$c_t = y_t + R_t x_{t-1} \quad (3)$$

- When y_t is large, self $t - 1$ will make x_{t-1} small to prevent self t from overconsuming.
- Self $t - 1$ can only deny self t access to assets that have been accumulated in the past, cannot deny access to y_t , labor income at time t

Co-Movement in Consumption and Income (continued)



Aggregate Savings

- Classical: High discount rates necessary condition for consumption-income co-movement. This implies low level of capital accumulation.
- Golden eggs model: Consumption-income co-movement even when actors are wealthy, since in equilibrium decision to dissave out of the illiquid asset stock is not dependent on β .
- Why? Self t is not able to consume from illiquid assets, so does not consider trade-off between consumption today and consumption tomorrow when dissaving from illiquid assets.

Asset-Specific MPCs

- Thaler (1990): people have mental accounts, different marginal propensities to consume (MPCs) for different categories of assets
- Thaler: 3 categories: current income (MPC ~ 1), net assets (MPC $0 < x < 1$), future income (MPC ~ 0)
- In golden eggs model current self is liquidity constrained on equilibrium path \rightarrow MPC out of current cash flow is 1 ($\frac{\partial c_t}{\partial (R_t x_{t-1})} = 1$)
- On equilibrium path self-imposed liquidity constraint \rightarrow MPC out of illiquid assets is 0 ($\frac{\partial c_t}{\partial (R_t z_{t-1})} = 0$)

Ricardian Equivalence

- Here, sequence of exogenous cash flows matters, independent of present value scheme. Taxation schemes affect these exogenous cash flows, so Ricardian equivalence is violated.

Declining U.S. Saving Rates in the 1980s

- Large proportion of national income realized as cash flow during that time period
- Special developments in consumer credit market → expansion in U.S. consumer credit market → commitment devices such as illiquid assets loose effectiveness, since one can generate credit loans on these illiquid assets
- Original model:

$$c_t \leq y_t + R_t x_{t-1} \quad (4)$$

- Now:

$$c_t \leq y_t + R_t x_{t-1} + R_t z_{t-1} \quad (5)$$

with instantaneous access to credit

What about Welfare?

- Instantaneous credit increases consumers' choice set,
- though eliminates possibility for partial commitment.
- Current self no longer liquidity constrained, can consume more in period of control, though can also consume more out of wealth stock
- First effect positive, second one is negative and usually dominant → people would not save enough

Evaluation

Problems with the model:

- How are assets accumulated in the first place
- Usually consumers do not consume all their liquid assets, but do hold some liquidity
- Some agents do have internal self-control and do not need commitment devices
- There may be social commitment devices (marriage, work, friendship etc.)

Hyperbolic Discounting and Savings

We discuss paper by O'Donoghue and Rabin (1999):

“Procrastination in Preparing for Retirement” (see also O'Donoghue and Rabin: “Doing it Now or Later”, AER, 1999)

- Hyperbolic discounting and self-control problems may cause undersaving
- A taste for immediate gratification can lead a person to sacrifice too much future consumption for the sake of current consumption → people end up with too little retirement savings
- People sophisticated and foresee that they will have self-control problems or rather naive and do not foresee the self-control problems? Or rational without any self-control problems?

The Model

- Intertemporal preferences:

$$U^t(u_t, u_{t+1}, \dots, u_T) = u_t + \beta \sum_{\tau=t+1}^T \delta^{\tau-t} u_{\tau}, \quad (6)$$

where $\delta \leq 1$ is the time-consistent discount factor and $\beta \leq 1$ is the bias for the present.

- Sophisticates: are aware of their future self-control problems
- Naifs: are fully unaware of their future self-control problems
- The rational investor: no time-inconsistency (TCs)

Loss from a τ -Delay

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$$L(\tau) = P\left[\left(1 + \frac{r_B}{365}\right)^T - \left(1 + \frac{r_A}{365}\right)^\tau \left(1 + \frac{r_B}{365}\right)^{T-\tau}\right] \quad (7)$$

where $r_B > r_A$ (rates of return on saving plan A, respectively B), $C > 0$ (transaction costs), P principal

- Hence, if in period t the person expects to incur transfer cost C in period $\tau \geq t$ and expects to retire in period $T + 1 \geq \tau$ with retirement savings S , then his period- t intertemporal utility is given by

$$U^t = \begin{cases} -C + \beta\delta^{T+1-t}S & \text{if } \tau = t \\ -\beta\delta^{\tau-t}C + \beta\delta^{T+1-t}S & \text{if } \tau > t \end{cases} \quad (8)$$

Lost Retirement Savings from Delay

Table 1: Lost Retirement Savings from Delay
(Principal = \$10,000, Horizon = 30 years)

r_A	r_B	Lost Retirement Savings from One-Day Delay ($L(1)$)	Lost Retirement Savings if Never Transfer ($L(T)$)
0%	1%	\$0.37	\$3,499
5%	6%	\$1.66	\$15,675
10%	11%	\$7	\$70,219
0%	5%	\$6	\$34,812
5%	10%	\$28	\$155,961
10%	15%	\$123	\$698,567
0%	10%	\$55	\$190,773
5%	15%	\$246	\$854,527
10%	20%	\$1,103	\$3,826,891

Now or Never

- More realistic: Plan B is more attractive the further one is from retirement, $\delta(1 + \frac{r_B}{365}) > 1$
- In this case, TCs and Naifs either transfer immediately or never.

Behavior of TCs

- Transfer funds immediately iff $C \leq \delta^T L(T)$
- Present discounted value of the extra interest is bigger than immediate cost of transferring the funds
- Never transfer funds iff $C > \delta^T L(T)$

Behavior of Naifs

- Unlike TCs, they do not compare transferring the funds now or never
- They constantly believe if they do not transfer the money today they will do so tomorrow.
- They only make the transfer iff doing so is preferred to a one-day delay.
- Thus, they prefer delaying iff $C > \beta\delta C + \beta\delta^T L(1)$
- i.e Transfer funds immediately iff $C \leq \frac{\beta}{1-\beta\delta}\delta^T L(1)$ or never transfer funds vice versa

Naifs' Procrastination on Daily Basis

Table 2: When Naifs Procrastinate: Single Alternative, Daily Decisions
(Principal = \$10,000, Horizon = 30 years)

r_A	r_B	δ^{365}	TCs never transfer funds if	Naifs	never	transfer	funds	if
				$\beta = .99$	$\beta = .98$	$\beta = .95$	$\beta = .90$	$\beta = .80$
0%	1%	.99	$C > 2,588$	$C > 27$	$C > 13$	$C > 5$	$C > 2$	$C > 1$
5%	6%	.99	$C > 11,595$	$C > 121$	$C > 60$	$C > 23$	$C > 11$	$C > 5$
		.96	$C > 4,606$	$C > 48$	$C > 24$	$C > 9$	$C > 4$	$C > 2$
10%	11%	.99	$C > 51,941$	$C > 542$	$C > 269$	$C > 104$	$C > 49$	$C > 22$
		.96	$C > 20,634$	$C > 214$	$C > 106$	$C > 41$	$C > 20$	$C > 9$
		.91	$C > 4,147$	$C > 42$	$C > 21$	$C > 8$	$C > 4$	$C > 2$
0%	5%	.99	$C > 25,751$	$C > 448$	$C > 222$	$C > 86$	$C > 41$	$C > 18$
		.96	$C > 10,230$	$C > 177$	$C > 88$	$C > 34$	$C > 16$	$C > 7$
5%	10%	.99	$C > 115,364$	$C > 2,008$	$C > 995$	$C > 386$	$C > 183$	$C > 81$
		.96	$C > 45,830$	$C > 791$	$C > 394$	$C > 153$	$C > 73$	$C > 32$
		.91	$C > 9,210$	$C > 157$	$C > 79$	$C > 31$	$C > 15$	$C > 6$
10%	15%	.99	$C > 516,730$	$C > 8,994$	$C > 4,457$	$C > 1,730$	$C > 820$	$C > 364$
		.96	$C > 205,279$	$C > 3,543$	$C > 1,764$	$C > 686$	$C > 325$	$C > 145$
		.91	$C > 41,252$	$C > 702$	$C > 352$	$C > 137$	$C > 65$	$C > 29$

Naifs' Procrastination on Weekly Basis

Table 3: When Naifs Procrastinate: Single Alternative, Weekly Decisions
(Principal = \$10,000, Horizon = 30 years)

r_A	r_B	δ^{365}	TCs never transfer funds if	Naifs				
				never $\beta = .99$	never $\beta = .98$	transfer $\beta = .95$	funds $\beta = .90$	if $\beta = .80$
0%	1%	.99	$C > 2,588$	$C > 186$	$C > 93$	$C > 36$	$C > 17$	$C > 8$
5%	6%	.99	$C > 11,595$	$C > 833$	$C > 416$	$C > 162$	$C > 77$	$C > 34$
		.96	$C > 4,606$	$C > 313$	$C > 161$	$C > 64$	$C > 30$	$C > 14$
10%	11%	.99	$C > 51,941$	$C > 3,733$	$C > 1,865$	$C > 727$	$C > 345$	$C > 154$
		.96	$C > 20,634$	$C > 1,403$	$C > 720$	$C > 286$	$C > 136$	$C > 61$
		.91	$C > 4,147$	$C > 258$	$C > 138$	$C > 56$	$C > 27$	$C > 12$
0%	5%	.99	$C > 25,751$	$C > 3,086$	$C > 1,542$	$C > 601$	$C > 285$	$C > 127$
		.96	$C > 10,230$	$C > 1,160$	$C > 596$	$C > 236$	$C > 113$	$C > 50$
5%	10%	.99	$C > 115,364$	$C > 13,825$	$C > 6,908$	$C > 2,694$	$C > 1,279$	$C > 569$
		.96	$C > 45,830$	$C > 5,195$	$C > 2,668$	$C > 1,058$	$C > 505$	$C > 225$
		.91	$C > 9,210$	$C > 954$	$C > 511$	$C > 209$	$C > 101$	$C > 45$
10%	15%	.99	$C > 516,730$	$C > 61,919$	$C > 30,939$	$C > 12,066$	$C > 5,726$	$C > 2,548$
		.96	$C > 205,279$	$C > 23,265$	$C > 11,949$	$C > 4,740$	$C > 2,263$	$C > 1,010$
		.91	$C > 41,252$	$C > 4,273$	$C > 2,291$	$C > 935$	$C > 451$	$C > 202$
0%	10%	.99	$C > 141,115$	$C > 27,639$	$C > 13,810$	$C > 5,386$	$C > 2,556$	$C > 1,137$
		.96	$C > 56,060$	$C > 10,385$	$C > 5,334$	$C > 2,116$	$C > 1,010$	$C > 451$
		.91	$C > 11,266$	$C > 1,907$	$C > 1,022$	$C > 417$	$C > 201$	$C > 90$
5%	15%	.99	$C > 632,094$	$C > 123,787$	$C > 61,853$	$C > 24,122$	$C > 11,448$	$C > 5,093$
		.96	$C > 251,109$	$C > 46,511$	$C > 23,888$	$C > 9,477$	$C > 4,524$	$C > 2,019$
		.91	$C > 50,462$	$C > 8,543$	$C > 4,579$	$C > 1,869$	$C > 901$	$C > 404$
10%	20%	.99	$C > 2,830,753$	$C > 554,302$	$C > 276,971$	$C > 108,015$	$C > 51,264$	$C > 22,806$
		.96	$C > 1,124,561$	$C > 208,271$	$C > 106,968$	$C > 42,437$	$C > 20,258$	$C > 9,039$
		.91	$C > 225,989$	$C > 38,253$	$C > 20,505$	$C > 8,368$	$C > 4,034$	$C > 1,809$

Behavior of Sophisticates

- A sophisticate correctly predicts behavior, thus, he will never make transfer iff on day 1 he prefers never making the transfer to making it immediately, thus $C > \beta\delta^T L(T)$

Sophisticates' Procrastination

Table 4: When Sophisticates Procrastinate Forever: Single Alternative, Daily Decisions
(Principal = \$10,000, Horizon = 30 years)

r_A	r_B	δ^{365}	TCs never transfer if	Sophisticates			
				never	transfer	never	transfer
				$\beta = .98$	$\beta = .95$	$\beta = .9$	$\beta = .8$
0%	1%	.99	$C > 2,588$	$C > 2,536$	$C > 2,458$	$C > 2,329$	$C > 2,070$
5%	6%	.99	$C > 11,595$	$C > 11,363$	$C > 11,015$	$C > 10,435$	$C > 9,276$
		.96	$C > 4,606$	$C > 4,514$	$C > 4,376$	$C > 4,146$	$C > 3,685$
10%	11%	.99	$C > 51,941$	$C > 50,902$	$C > 49,344$	$C > 46,747$	$C > 41,553$
		.96	$C > 20,634$	$C > 20,222$	$C > 19,603$	$C > 18,571$	$C > 16,507$
		.91	$C > 4,147$	$C > 4,064$	$C > 3,939$	$C > 3,732$	$C > 3,317$
0%	5%	.99	$C > 25,751$	$C > 25,236$	$C > 24,463$	$C > 23,176$	$C > 20,601$
		.96	$C > 10,230$	$C > 10,025$	$C > 9,718$	$C > 9,207$	$C > 8,184$
5%	10%	.99	$C > 115,364$	$C > 113,057$	$C > 109,596$	$C > 103,828$	$C > 92,291$
		.96	$C > 45,830$	$C > 44,914$	$C > 43,539$	$C > 41,247$	$C > 36,664$
		.91	$C > 9,210$	$C > 9,026$	$C > 8,749$	$C > 8,289$	$C > 7,368$
10%	15%	.99	$C > 516,730$	$C > 506,395$	$C > 490,894$	$C > 465,057$	$C > 413,384$
		.96	$C > 205,279$	$C > 201,174$	$C > 195,015$	$C > 184,751$	$C > 164,223$
		.91	$C > 41,252$	$C > 40,427$	$C > 39,190$	$C > 37,127$	$C > 33,002$
0%	10%	.99	$C > 141,115$	$C > 138,292$	$C > 134,059$	$C > 127,003$	$C > 112,892$
		.96	$C > 56,060$	$C > 54,939$	$C > 53,257$	$C > 50,454$	$C > 44,848$
		.91	$C > 11,266$	$C > 11,040$	$C > 10,702$	$C > 10,139$	$C > 9,013$
5%	15%	.99	$C > 632,094$	$C > 619,452$	$C > 600,489$	$C > 568,885$	$C > 505,675$
		.96	$C > 251,109$	$C > 246,087$	$C > 238,554$	$C > 225,998$	$C > 200,888$
		.91	$C > 50,462$	$C > 49,453$	$C > 47,939$	$C > 45,416$	$C > 40,370$
10%	20%	.99	$C > 2,830,753$	$C > 2,774,138$	$C > 2,689,215$	$C > 2,547,678$	$C > 2,264,602$
		.96	$C > 1,124,561$	$C > 1,102,070$	$C > 1,068,333$	$C > 1,012,105$	$C > 899,649$
		.91	$C > 225,989$	$C > 221,470$	$C > 214,690$	$C > 203,390$	$C > 180,791$

Alternative Investments

- Costless transfer from plan A to plan B with $r_B > r_A$, or transfer from plan A to plan C with cost C and $r_C > r_B$
- Again $\delta(1 + \frac{r_B}{365}) > 1$

Behavior of TCs

- Transfer to plan C at $\tau = 1$ iff

$$\delta^T P \left[\left(1 + \frac{r_C}{365}\right)^T - \left(1 + \frac{r_B}{365}\right)^T \right] \geq C$$

- Transfer to plan B at $\tau = 1$ iff

$$\delta^T P \left[\left(1 + \frac{r_C}{365}\right)^T - \left(1 + \frac{r_B}{365}\right)^T \right] < C$$

Behavior of Naifs

Three options: choose plan B today, choose plan C today, plan to choose plan C tomorrow (plan B today dominates plan B tomorrow since no costs apply). These plans yield utility of:

- Plan B today: $\beta\delta^{T+1-\tau}P\left(1 + \frac{r_A}{365}\right)^{\tau-1}\left(1 + \frac{r_B}{365}\right)^{T+1-\tau} - 0$
- Plan C today: $\beta\delta^{T+1-\tau}P\left(1 + \frac{r_A}{365}\right)^{\tau-1}\left(1 + \frac{r_C}{365}\right)^{T+1-\tau} - C$
- Plan C tomorrow: $\beta\delta^{T+1-\tau}P\left(1 + \frac{r_A}{365}\right)^{\tau}\left(1 + \frac{r_C}{365}\right)^{T-\tau} - \beta\delta C$

TCs and Naifs

- If TCs prefer plan B and think that plan C requires too much effort - so will Naifs, and since plan B is costless, if Naifs plan to choose B, they will do so immediately.
- What if TCs choose plan C? Assume Naifs prefer plan C to plan B today, then plan B irrelevant for Naifs' decision → relevant is only plan C today or plan C tomorrow.
- This means we are back at same problem as before - the best action is the unique action.
- Introducing a costless option does not necessarily overturn procrastination.
- But not forever - as time goes by, benefit of plan C compared to plan B decreases → eventually investment in plan B (since it is costless).

Transfer of Funds - Alternatives

Table 7: When People Transfer Funds: Choice of Alternatives
 (Principal = \$10,000, Horizon = 30 years)

r_A	r_B	r_C	C	δ^{365}	TCs	β^c	Naifs If $\beta > \beta^c$	If $\beta < \beta^c$
0%	5%	6%	500	.99	Plan C on day 1	.986	Plan C on day 1	Plan B at 25.8 yrs
			500	.96	Plan C on day 1	.994	Plan C on day 1	Plan B at 25.3 yrs
			2000	.96	Plan C on day 1	.999	Plan C on day 1	Plan B at 14.0 yrs
0%	7%	8%	500	.99	Plan C on day 1	.966	Plan C on day 1	Plan B at 26.1 yrs
			500	.96	Plan C on day 1	.986	Plan C on day 1	Plan B at 25.7 yrs
			2000	.96	Plan C on day 1	.997	Plan C on day 1	Plan B at 17.1 yrs
0%	10%	11%	500	.99	Plan C on day 1	.892	Plan C on day 1	Plan B at 26.4 yrs
			500	.96	Plan C on day 1	.954	Plan C on day 1	Plan B at 26.1 yrs
			500	.91	Plan C on day 1	.991	Plan C on day 1	Plan B at 25.2 yrs
			2000	.96	Plan C on day 1	.988	Plan C on day 1	Plan B at 19.7 yrs

Implications for Policy

- Status-quo bias
- Thus firms may choose default investment
- High sensitivity to short-run incentives
- Tax incentives
- Impose dead-lines - for example less frequent transaction dates
- Improve information

Example: Save More Tomorrow

Thaler and Benartzi: Save More Tomorrow: Using Behavioral Economics to Increase Employee Saving

- Design of pension plans
- Save More Tomorrow (SMT) program - workers are given the option to commit future raises in salary to savings
- If workers are already choosing their life-cycle savings rate optimally, they have no incentive to join a program that will commit them to periodic changes.

Example: Save More Tomorrow (continued)

- Lag between sign-up and start-up date should be as long as feasible.
- If employees join, their contribution to the plan is increased beginning with the first paycheck after a raise. This feature mitigates the perceived loss aversion of a cut in take-home pay.
- Contribution rate continues to increase on each scheduled raise until the contribution rate reaches a preset maximum. In this way, inertia and status quo bias work towards keeping people in the plan.
- Employee can opt out of the plan at any time.

References

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- [3] **Thaler, Richard H. and Benartzi, Shlomo (2004):** “Save More Tomorrow: Using Behavioral Economics to Increase Employee Saving,” *Journal of Political Economy*, 112, S164-S187.